Reducing the Fiber Non-linearities by Mitigating the PAPR in Optical OFDM Systems

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Abstract: *Orthogonal Frequency Division Multiplexing (OFDM) plays a vital role in many wireless network applications. However, it has a huge drawback called as higher peak to average power ratio (PAPR), which in results increases the complexity of digital to analog converters (DAC) and analog to digital converters (ADC) and also degrades the efficiency of high power amplifiers (HPA). Here, we have implemented non-linearities reduction in optical- OFDM (O-OFDM) system by mitigating the PAPR. Simulation results have shown that the proposed algorithm has performed superior results over the conventional algorithms and original OFDM system.*

Keywords: *OFDM, PAPR, non-linear companding, smoothing function and optical- OFDM (O-OFDM)*

I. Introduction

Due to the multipath fading effect and receiver many-sided quality of wireless channels, the conventional modulation techniques which depend on single carrier can accomplish restricted data rates. High data-rate is attractive in numerous late wireless multimedia applications [1]. Be that as it may, as the data-rate in correspondence framework expands, the symbol duration gets lessened. In this manner, the correspondence frameworks utilizing single carrier modulation experience the ill effects of serious inter symbol interference (ISI) created by dispersive channel drive reaction, in this way requiring a mind boggling balance component. Orthogonal Frequency Division Multiplexing (OFDM) is an exceptional type of multicarrier modulation strategy, in which the total Frequency specific fading channel will be separated into numerous orthogonal slender band level fading sub channels. In OFDM framework high-piece rate data stream is transmitted in parallel over various lower data rate subcarriers and don't experience ISI because of the long symbol duration [2]. Significant favourable circumstances of OFDM frameworks are

➤ High ghastly effectiveness.
➤ Simple computerized acknowledgment by utilizing the FFT operation.
➤ Due to the ISI evasion, the many-sided quality in the receiver will be decreased.
➤ Various modulation plans will be utilized to accomplish the best execution of the framework.

Because of the previously mentioned favorable circumstances, OFDM has been utilized as a part of numerous wireless applications, for example, Wireless Personal Area Network (WPAN), Wireless Local Area Network (WLAN) [4], Wireless Metropolitan Area Network (WMAN), Digital Audio Broadcasting (DAB) [3] and Digital Video Broadcasting (DVB) [5]. It is likewise being considered for IEEE 802.20, 802.16 [6], [7] and 3GPP-LTE. With the utilization of cyclic prefix for killing the effect of ISI, there is a requirement for a basic one tap equalizer at the OFDM receiver. OFDM gets unparalleled transmission capacity funds, which prompts to high otherworldly proficiency. Regardless of the across the board acknowledgment of OFDM, it has its downsides:

➤ OFDM signals with high peak-to-average power ratio (PAPR) prompts to the corruption in framework execution, which in results the improved out-of-band power.
➤ OFDM frameworks are touchier to Doppler spread when contrasted with single carrier modulation plans.
➤ The framework execution will be corrupted by the stage clamor, which is brought about by the blemishes of the transmitter and receiver.
➤ It requires precise time and Frequency synchronization.
➤ Due to the cyclic prefix (CP) it loses phantom proficiency.

As recorded above, huge envelope vacillation in OFDM flag is one of the real disadvantages of OFDM. Such vacillations make challenges on the grounds that useful correspondence frameworks are peak power restricted. Hence, envelope peaks require a framework to suit a momentary flag power that is bigger than the flag average power, requiring either low working power efficiencies or power amplifier (PA) saturation. Keeping in mind the end goal to increase the OFDM motion with huge envelope changes, PAs with substantial direct range are required, which makes it extremely costly. In the event that PA has restricted straight range then its operation in non-direct mode presents out of band radiation and in band distortion. It is additionally important to have D/An and A/D converters with huge element range to change over discrete time OFDM flag to simple flag and the other way around.

II. Related Work

From the previous decades numerous PAPR diminishment techniques have been proposed to enhance the advanced correspondence framework effectiveness, and still the analysts are concentrating on creating broadened PAPR decrease plans with more effective outcomes. Among them, couple of techniques like piece coding plans [8], Tone Reservation (TR), Tone Injection (TI) [10-12], iterative cutting and separating [16], Partial Transmit Sequence (PTS) [9], Active Constellation Extension (ACE) [11], Adaptive ACE [12-14], Select Level Mapping (SLM) [19], companding techniques, for example, straight [10], non-direct, exponential companding [15] are more prevalent. The letter proposed in [8] gives a piece coding strategy for PAPR decrease of multi carrier transmission strategies, for example, OFDM. In this approach the creator has utilized ¾ rate square code and reenacted this with a case of four-carrier flag furthermore with eight-carrier flag. Be that as it may, piece coding plan has diminished peak to mean conceal power ratio (PMEPR) yet it has the restriction in number of carriers, thus does not suit for longer data arrangements. X. Li et. al. in [9] proposed another PAPR decrease plot which depends on section and sifting, which diminishes the peak to mean encompass power ratio by cut-out the transmitted arrangement to certain degree and a short time later channels the cut data to lessen the PAPR. In spite of the fact that it lessens the PAPR to some degree yet while cutting the info data we are losing the first data bits, which in results the poor framework productivity. Wattanasuwakull et. al. proposed tone reservation (TR) and tone infusion (TI) technique [10] to decrease the PAPR of the OFDM flag. Fundamental thought of the approach in [11] is to create a surplus and direct flag which will lessen the peak-power by reservation of number of subcarriers. In any case, because of the surplus symbols and the bigger flag heavenly body use it backs off the data rate and expands transmitter power. Sang et. al. in [13] proposed a changed particular mapping plan (SLM) to lessen the PAPR which performs superior to ordinary SLM and PTS. Calculation in [13] proposes an altered SLM in which the subcarriers which are predefined will be embedded by the sham or reciprocal succession taken from flipping strategy. Fractional Transmit Sequences (PTS) is an effective method for diminishment of Peak-to-Average Power Ratio (PAPR) Orthogonal Frequency Division Multiplexing (OFDM) framework. In any case, higher computational multifaceted nature is the significant disadvantage of PTS. With a specific end goal to beat this numerous PTS strategies have been proposed. The paper proposed in [14] talks about the advanced PTS (O-PTS) plot with super forced preparing, in which the O-PTS technique diminishes the PAPR to 7.25 dB from 10 dB of customary PTS conspire. In [15] change based approach for PAPR lessening has been proposed, which utilizes direct companding change. Another approach of PAPR decrease proposed in [16], which exhibits another crossover peak-to-average power ratio lessening strategy with the mix of ACE and TR. As of late, versatile dynamic group of stars augmentation (AACE) strategy has been proposed in [17-18]. In this approach AACE beats the disadvantages of the existed ACE and cutting based dynamic heavenly body augmentation (CB-ACE). In [20] the creator attempted to clarify the companding OFDM techniques to decrease the PAPR. Companding techniques have the preferred execution over the ACE, AACE yet it underpins constrained modulation plans and it experiences extensive level of companding quality However, every one of the strategies which have been talked about above have numerous downsides. To beat every one of the downsides of traditional plans here in this paper we presented a novel plan which is based sin and cosine pre-coding (SCP) algorithm for O-OFDM to mitigate the fiber non-linearities. This system is proficient, flag free, distortion less, it doesn't require any improvement calculation and PAPR is totally dispensed with.

A.   PAPR in OFDM Systems

Input data sequence to be transmitted with N subcarriers in an OFDM symbol is $(0),(1), \cdots, X(N-1)$. The baseband representation of the OFDM symbol is given by:

$$x(t) = \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} X(n) e^{\frac{j2\pi nt}{N}} \quad 0 \leq t \leq T \quad (1)$$

T is OFDM symbol duration. When N value will be increased then both the real and imaginary parts of $x(t)$ would become Gaussian distributed and each with zero mean with a variance of $E[|x(t)^2|]/2$, and the OFDM symbol amplitude follows a Rayleigh distribution. Therefore, it is possible that the OFDM symbol amplitude will be exceeds than the maximum amplitude. Practical hardware such as A/D and D/A converters, high power amplifiers (HPA) has finite dynamic range; therefore the maximum amplitude of OFDM signal should be limited. PAPR of an OFDM signal has been defined as:

$$PAPR = \frac{\max[|x(t)^2|]}{\frac{1}{T}\int_0^T |x(t)|^2 dt} \quad (2)$$

In dB value the PAPR can be written as $PAPR = 10\log_{10}(PAPR)$. It is easy to see from (2) that reduction of PAPR can be achieved by reducing the numerator and increasing the denominator, or both. Complementary

cumulative distributed function (CCDF) will be used as a measurement of PAPR effectiveness, which is the probability that PAPR exceeds some threshold, i.e.,

$$CCDF = Probability\ (PAPR > p_0) \qquad (3)$$

where p_0 is the threshold.

B. New Companding Algorithm

Let a non-linear companding function is $f(x)$, and $x(t) = \sin(\omega t)$ be the compander input, then the companded signal $y(t)$ can be written as:

$$y(t) = f[x(t)] = f[\sin(\omega t)] \qquad (4)$$

The companding algorithm uses a smooth function named as airy function to reduce the peak value. The companding function is as follows:

$$f(x) = \beta.\,sign(x).\,[airy(0) - airy(\alpha.\,|x|)] \qquad (5)$$

Where $airy(.)$ is the airy function, β is the adjusting factor for the average output power of the compander to the same level of input power.

$$\beta = \sqrt{\frac{E[|x|^2]}{E[|airy(0) - airy(\alpha.|x|)|^2]}} \qquad (6)$$

Here E [.] denotes the expectation.

III. Proposed Algorithm

Generally, the SCP is an invertible function H: $\mathbf{R}^n \rightarrow \mathbf{R}^n$ (where $\mathbf{R}$ denotes the set of real numbers) and it is a linear function. The N real numbers $x_0, ..., x_{N-1}$ are transformed into the N real numbers $H_0, ..., H_{N-1}$.
The Pre-coding matrix P can be written as

$$P = \begin{bmatrix} p_{00} & p_{01} & ... & p_{0(N-1)} \\ p_{10} & p_{11} & ... & p_{1(N-1)} \\ \vdots & \vdots & \ddots & \vdots \\ p_{(N-1)0} & p_{(N-1)1} & ... & p_{(N-1)(N-1)} \end{bmatrix}$$

Where P is a Pre-coding Matrix of size N×N is shown in above equation. The complex baseband OFDM signal with N sub carriers can be written as

$$x(t) = \frac{1}{\sqrt{N}} \sum_{k=0}^{N-1} P.X_k\ e^{j2\pi k \Delta ft},$$
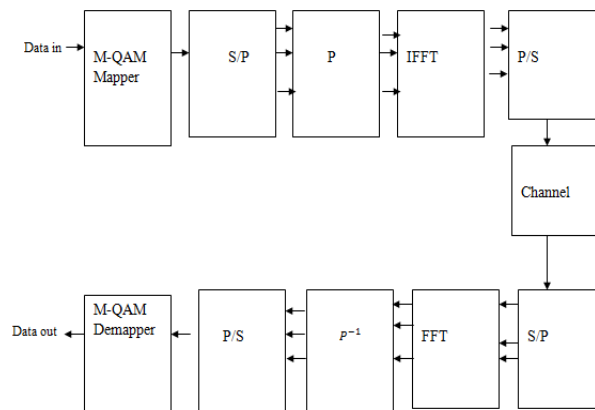$$0 \leq t \leq NT \qquad (7)$$

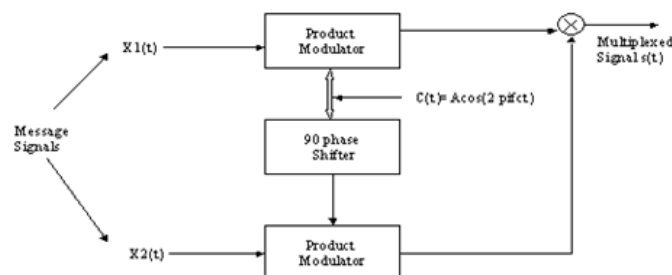**Fig.1** O-OFDM system with pre-coding matrix

Fig.2 QAM system

We can express modulated O-OFDM vector signal with N subcarriers as follows:

$$x_N = IFFT\{P.X_N\} \tag{8}$$

The SCP is a linear transform and N-point SCP can be defined as:

$$H_k = \sum_{n=0}^{N-1} x_n \left[\cos\left(\frac{2\pi nk}{N}\right) + \sin\left(\frac{2\pi nk}{N}\right)\right]$$

$$= \sum_{n=0}^{N-1} x(n).cas\left(\frac{2\pi nk}{N}\right) \tag{9}$$

Where $cas\ \theta = \cos\theta + \sin\theta$ and $k = 0, 1, \ldots N-1$

$$p_{m,n} = cas\left(\frac{2\pi mn}{N}\right) \tag{10}$$

P is pre-coding matrix of size N×N. and both (m, n) are integers from range 0 to N-1. The SCP is also invertible transform which allows us to recover the X_n from H_k and inverse can be obtained by simply multiplying SCP of H_k by 1/N. In this, we analyzed the performance of SC Pre-coding matrix for the reduction of fiber non-linearities in high speed O-OFDM systems using M-QAM constellation modulation scheme (where M=16, 32, 64, 128 and so on). Additionally, it does not require any power increment, complex optimization and side information to be sent for the receiver.

IV. Simulation Results

Experimental results have been done in MATLAB tool. Table 1 show that the simulation parameters considered for executing the reduction of fiber non-linearities in O-OFDM system. Figure3 (a) and (b) shown that the comparison of degree of companding for the algorithm proposed in [20], which is a conventional scheme. Magnitude, phase and estimation of magnitude responses of proposed and conventional schemes has been shown in figure 4, 5 and 6 respectively. Figure 7 shows that the round-off noise power spectrum of proposed and conventional schemes. Non-linearities reduction in O-OFDM has been compared in figure 8 by reducing the PAPR using conventional schemes, it shows that the exponential companding got the PAPR of 3.85 dB, scheme proposed in [20] got 4.25 dB and 12 dB for original O-OFDM system i.e., without using any of PAPR reduction algorithm.
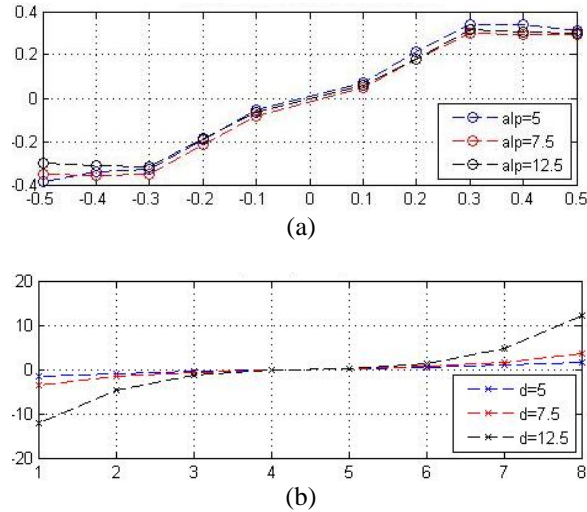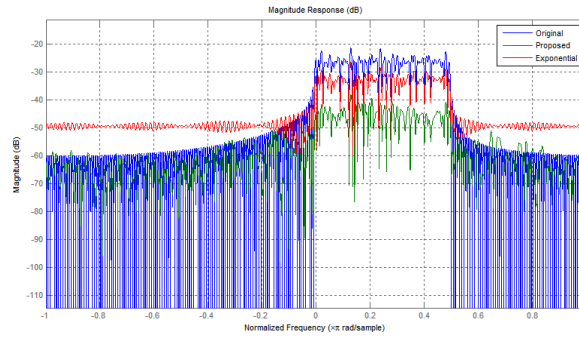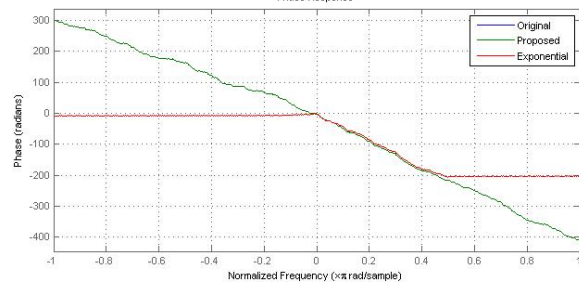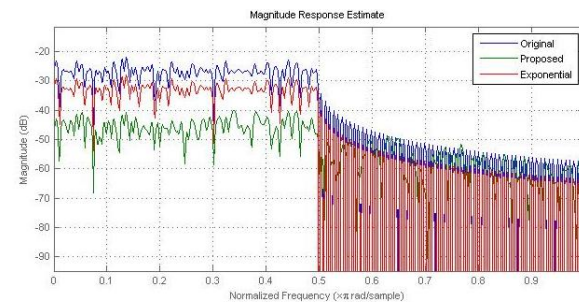

(a)

(b)

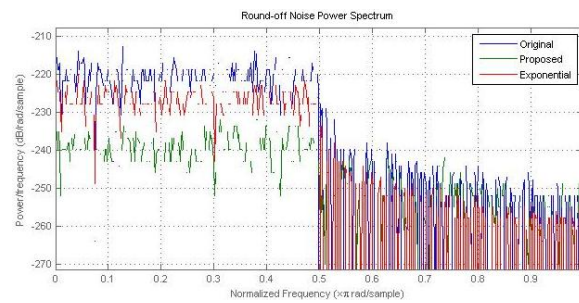**Fig.3** degree of companding comparison for scheme proposed in [20]

Fig.4 Magnitude response

Fig.5 Phase response

Fig.6 Estimation of magnitude response

Fig.7 Round-off Noise Power Spectrum

PAPR reduction of proposed SCP algorithm has been shown in figure 9. We have reduced it to 0.69 dB which is very lesser value over the all conventional reduction schemes proposed in the literature. Therefore, our proposed algorithm has reduced the non-linearities of fiber in optical OFDM systems to maximum extend. Finally, we have compared the bit error rate performance of proposed and conventional schemes to achieve higher speed data rates for O-OFDM.
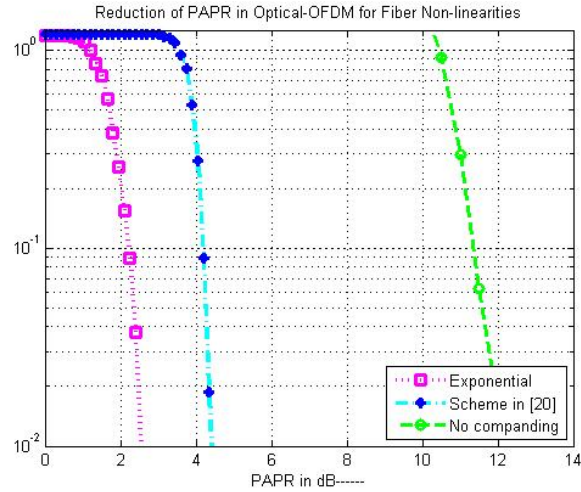
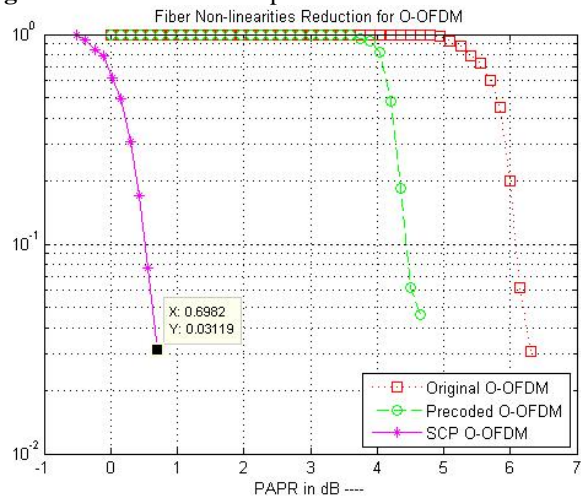**Fig.8** PAPR reduction comparison of conventional schemes

Fig.9 Reduction of PAPR using conventional and SCP for O-OFDM

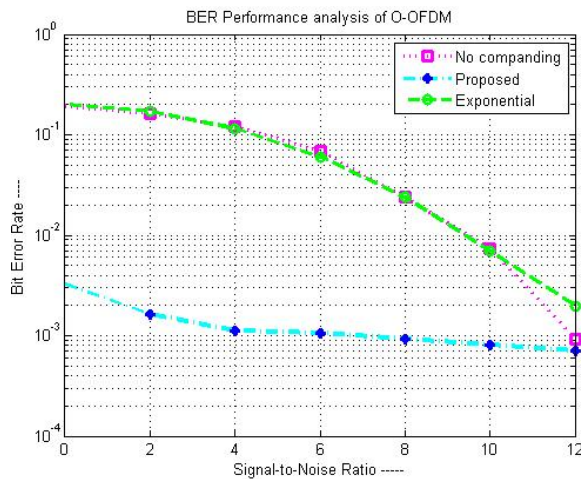**Fig.10** Comparison of BER performance for O-OFDM

Table I: Simulation parameters

Parameters	Specifications
FFT & IFFT size	256
No. of Subcarriers	512
alpha	30 dB
Channel model	AWGN
Modulation scheme	QAM

Constellation points	4, 8, 16, and so on

V. Conclusion

In this letter, we analyzed the performance of fiber non-linearities reduction schemes in O-OFDM system using M-QAM constellation modulation (where M=16, 32, 64, 128 and so on). The simulation results, which have been implemented in MATLAB shows that the proposed SCP algorithm has got the better performance than the conventional schemes. Thus, it is concluded that proposed system shows maximum reduction of fiber non-linearities than conventional reduction techniques. Additionally, it does not require any power increment, complex optimization and side information to be sent for the receiver.

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